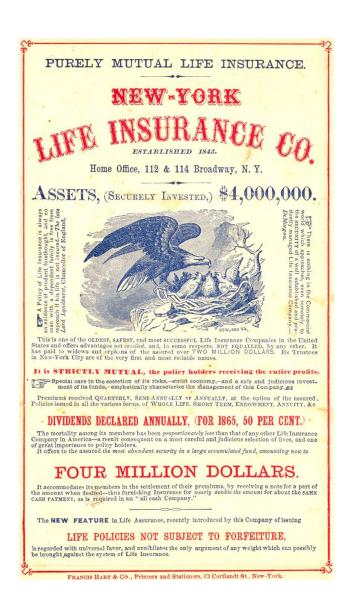
## **Competitive insurance markets** in a context of big data and machine learning

A. Charpentier (Université de Rennes 1)

Bank of England, London November 2017





#### **Brief Introduction**

A. Charpentier (Université de Rennes 1)

Professor Economics Department, Université de Rennes 1
Director Data Science for Actuaries Program, Institute of Actuaries
(previously Actuarial Sciences, UQàM & ENSAE Paristech
actuary in Hong Kong, IT & Stats FFA)

PhD in Statistics (KU Leuven), Fellow of the Institute of Actuaries MSc in Financial Mathematics (Paris Dauphine) & ENSAE

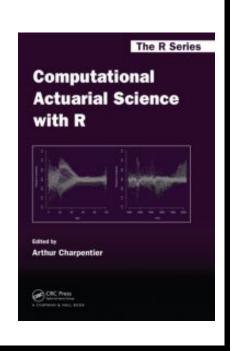
Research Chair:

ACTINFO (valorisation et nouveaux usages actuariels de l'information)

Editor of the freakonometrics.hypotheses.org's blog

Editor of Computational Actuarial Science, CRC

Author of Mathématiques de l'Assurance Non-Vie (2 vol.), Economica





Insurance vs. Credit

click to visualize the construction











#### **Insurance Pricing in a Nutshell**

Insurance is the contribution of the many to the misfortune of the few

Finance: risk neutral valuation  $\pi = \mathbb{E}_{\mathbb{Q}}[S_1 | \mathcal{F}_0] = \mathbb{E}_{\mathbb{Q}_0}[S_1]$ , where  $S_1 = \sum_{i=1}^r Y_i$ 

Insurance: risk sharing (pooling)  $\pi = \mathbb{E}_{\mathbb{P}}[S_1]$ 

or, with segmentation / price differentiation  $\pi(\omega) = \mathbb{E}_{\mathbb{P}}[S_1 | \Omega = \omega]$  for some (unobservable?) risk factor  $\Omega$ 

imperfect information given some (observable) risk variables  $\boldsymbol{X} = (X_1, \dots, X_k)$  $\boldsymbol{\pi}(\boldsymbol{x}) = \mathbb{E}_{\mathbb{P}}[S_1 | \boldsymbol{X} = \boldsymbol{x}] = \mathbb{E}_{\mathbb{P}_{\boldsymbol{X}}}[S_1 | \boldsymbol{x}]$ 

Insurance pricing is not only data driven, it is also essentially model driven (see Pricing Game)



## **Insurance Pricing in a Nutshell**

Premium is  $\pi = \mathbb{E}_{\mathbb{P}_{\boldsymbol{X}}}[S_1]$ 

It is datadriven (or portfolio driven) since  $\mathbb{P}_{\boldsymbol{X}}$  is based on the portfolio.

click to visualize the construction

#### **Insurance Pricing in a Nutshell**

Premium is 
$$\pi \approx \mathbb{E}[S_1 | \boldsymbol{X} = \boldsymbol{x}] = \mathbb{E}\left[\sum_{i=1}^N Y_i \middle| \boldsymbol{X} = \boldsymbol{x}\right] = \mathbb{E}[N | \boldsymbol{X} = \boldsymbol{x}] \cdot \mathbb{E}[Y_i | \boldsymbol{X} = \boldsymbol{x}]$$

Statistical and modeling issues to approximate based on some training datasets, with claims frequency  $\{n_i, \boldsymbol{x}_i\}$  and individual losses  $\{y_i \boldsymbol{x}_i\}$ 

- depends on the model used to approximate  $\mathbb{E}[N|X=x]$  and  $\mathbb{E}[Y_i|X=x]$
- depends on the choice of meta-parameters
- depends on variable selection / feature engineering

Try to avoid overfit

actinfo.

## **Risk Sharing in Insurance**

Important formula  $\mathbb{E}[S] = \mathbb{E}[\mathbb{E}[S|X]]$  and its empirical version

$$\frac{1}{n} \sum_{i=1}^{n} S_i \sim \frac{1}{n} \sum_{i=1}^{n} \pi(\boldsymbol{X}_i) \quad (\text{as } n \to \infty, \text{ from the law of large number})$$

interpreted as on average what we pay (losses) is the sum of what we earn (premiums).

This is an ex-post statement, where premiums were calculated ex-ante.



## **Risk Transfert without Segmentation**

	Insured	Insurer
Loss	$\mathbb{E}[S]$	$S - \mathbb{E}[S]$
Average Loss	$\mathbb{E}[S]$	0
Variance	0	$\operatorname{Var}[S]$

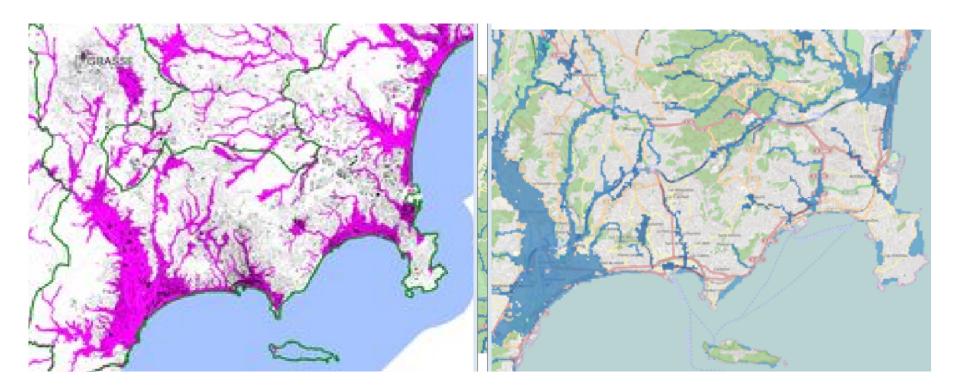
All the risk - Var[S] - is kept by the insurance company.

Remark: all those interpretation are discussed in Denuit & Charpentier (2004).



#### Insurance, Risk Pooling and Solidarity

"La Nation proclame la solidarité et l'égalité de tous les Français devant les charges qui résultent des calamités nationales" (alinéa 12, préambule de la Constitution du 27 octobre 1946)



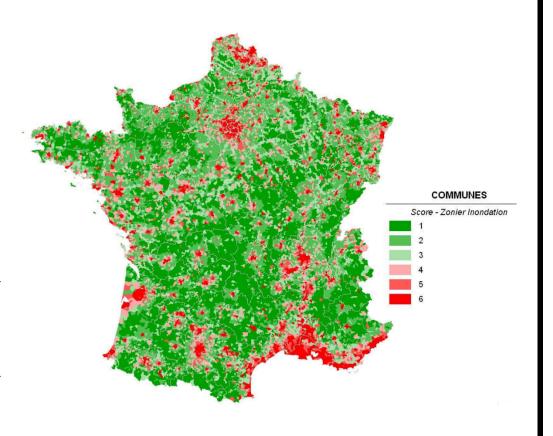
31 zones TRI (Territoires à Risques d'Inondation) on the left, and flooded areas.

## Insurance, Risk Pooling and Solidarity

Here is a map with a risk score -  $\{1, 2, \dots, 6\}$  scale

One can look at "Lorenz curve"

	South	Other	Total
% portfolio	11%	89%	100%
% claims	51%	49%	100%
Premium	463	55	100





## Risk Transfert with Segmentation and Perfect Information

Assume that information  $\Omega$  is observable,

	Insured	Insurer
Loss	$\mathbb{E}[S oldsymbol{\Omega}]$	$S - \mathbb{E}[S oldsymbol{\Omega}]$
Average Loss	$\mathbb{E}[S]$	0
Variance	$\operatorname{Var}\!\left[\mathbb{E}[S oldsymbol{\Omega}] ight]$	$\mathrm{Var} ig[ S - \mathbb{E}[S   oldsymbol{\Omega}] ig]$

Observe that 
$$\operatorname{Var} \left[ S - \mathbb{E}[S|\Omega] \right] = \mathbb{E}\left[ \operatorname{Var}[S|\Omega] \right]$$
, so that

$$\operatorname{Var}[S] = \underbrace{\mathbb{E}\left[\operatorname{Var}[S|\Omega]\right]}_{\rightarrow \text{ insurer}} + \underbrace{\operatorname{Var}\left[\mathbb{E}[S|\Omega]\right]}_{\rightarrow \text{ insured}}.$$



#### Risk Transfert with Segmentation and Imperfect Information

Assume that  $X \subset \Omega$  is observable

	Insured	Insurer
Loss	$\mathbb{E}[S oldsymbol{X}]$	$S - \mathbb{E}[S oldsymbol{X}]$
Average Loss	$\mathbb{E}[S]$	0
Variance	$\mathrm{Var}\Big[\mathbb{E}[S oldsymbol{X}]\Big]$	$\mathbb{E}\Big[\mathrm{Var}[S oldsymbol{X}]\Big]$

Now

$$\mathbb{E}\left[\operatorname{Var}[S|\boldsymbol{X}]\right] = \mathbb{E}\left[\mathbb{E}\left[\operatorname{Var}[S|\boldsymbol{\Omega}]\big|\boldsymbol{X}\right]\right] + \mathbb{E}\left[\operatorname{Var}\left[\mathbb{E}[S|\boldsymbol{\Omega}]\big|\boldsymbol{X}\right]\right]$$

$$= \mathbb{E}\left[\operatorname{Var}[S|\boldsymbol{\Omega}]\right] + \mathbb{E}\left\{\operatorname{Var}\left[\mathbb{E}[S|\boldsymbol{\Omega}]\big|\boldsymbol{X}\right]\right\}.$$
pooling solidarity



## Risk Transfert with Segmentation and Imperfect Information

With imperfect information, we have the popular risk decomposition

$$\operatorname{Var}[S] = \mathbb{E}\left[\operatorname{Var}[S|\boldsymbol{X}]\right] + \operatorname{Var}\left[\mathbb{E}[S|\boldsymbol{X}]\right]$$

$$= \mathbb{E}\left[\operatorname{Var}[S|\boldsymbol{\Omega}]\right] + \mathbb{E}\left[\operatorname{Var}\left[\mathbb{E}[S|\boldsymbol{\Omega}]|\boldsymbol{X}\right]\right]$$

$$\xrightarrow{\text{pooling}} \quad \text{solidarity}$$

$$\rightarrow \text{insurer}$$

$$+ \operatorname{Var}\left[\mathbb{E}[S|\boldsymbol{X}]\right].$$

$$\rightarrow \text{insured}$$



#### More and more price differentiation?

Consider 
$$\pi_1 = \mathbb{E}[S_1]$$
 and  $\pi_2(\boldsymbol{x}) = \mathbb{E}[S_1|\boldsymbol{X} = \boldsymbol{x}]$   
Observe that  $\mathbb{E}[\pi(\boldsymbol{X})] = \sum_{\boldsymbol{x} \in \mathcal{X}} \pi(\boldsymbol{x}) \cdot \mathbb{P}[\boldsymbol{x}]$   
 $= \sum_{\boldsymbol{x} \in \mathcal{X}_1} \pi(\boldsymbol{x}) \cdot \mathbb{P}[\boldsymbol{x}] + \sum_{\boldsymbol{x} \in \mathcal{X}_2} \pi(\boldsymbol{x}) \cdot \mathbb{P}[\boldsymbol{x}]$ 

- Insured with  $x \in \mathcal{X}_1$ : choose Ins1
- Insured with  $x \in \mathcal{X}_2$ : choose Ins2

$$\begin{array}{l} \text{Ins1: } \sum_{\boldsymbol{x}\in\mathcal{X}_1}\pi_1(\boldsymbol{x})\cdot\mathbb{P}[\boldsymbol{x}]\neq\mathbb{E}[S|\boldsymbol{X}\in\mathcal{X}_1]\\ \\ \text{Ins2: } \sum_{\boldsymbol{x}\in\mathcal{X}_2}\pi_2(\boldsymbol{x})\cdot\mathbb{P}[\boldsymbol{x}]=\mathbb{E}[S|\boldsymbol{X}\in\mathcal{X}_2] \end{array}$$





## **Price Differentiation, a Toy Example**

Claims frequency Y (average cost = 1,000)

			$X_1$		
		Young	Experienced	Senior	Total
	Town	12%	9%	9%	9.5%
$X_2$	Town	(500)	(2,000)	(500)	(3,000)
	Outside	8%	6.67%	4%	6.33%
	Outside	(500)	(1,000)	(500)	(2,000)
	Total	10%	8.22%	6.5%	8.23%
10tai	(1,000)	(3,000)	(1,000)	(5,000)	

from C., Denuit & Élie (2015)

## **Price Differentiation, a Toy Example**

	Y-T	Y-O	E-T	E-O	S-T	S-O
	(500)	(500)	(2,000)	(1,000)	(500)	(500)
none	82.3	82.3	82.3	82.3	82.3	82.3
$X_1 \times X_2$	120	80	90	66.7	90	40
market	82.3	80	82.3	66.7	82.3	40
none	82.3	82.3	82.3	82.3	82.3	82.3
$X_1$	100	100	82.2	82.2	65	65
$X_2$	95	63.3	95	63.3	95	63.3
$X_1 \times X_2$	120	80	90	66.7	90	40
market	82.3	63.3	82.2	63.3	65	40



## **Price Differentiation, a Toy Example**

	premium	losses	loss		99.5%	Market
			ratio		quantile	Share
none	247	285	115.4%	$(\pm 8.9\%)$		66.1%
$X_1 \times X_2$	126.67	126.67	100.0%	$(\pm 10.4\%)$		33.9%
market	373.67	411.67	110.2%	$(\pm 5.1\%)$		
none	41.17	60	145.7%	$(\pm 34.6\%)$	189%	11.6%
$X_1$	196.94	225	114.2%	$(\pm 11.8\%)$	140%	55.8%
$X_2$	95	106.67	112.3%	$(\pm 15.1\%)$	134%	26.9%
$X_1 \times X_2$	20	20	100.0%	$(\pm 41.9\%)$	160%	5.7%
market	353.10	411.67	116.6%	$(\pm 5.3\%)$	130%	

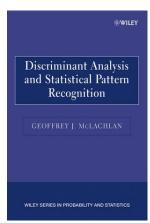


## Model Comparison (and Inequalities)

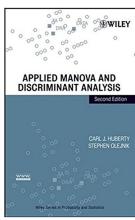
Use of statistical techniques to get price differentiation see discriminant analysis, Fisher (1936)

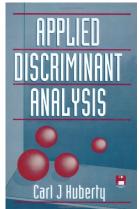
"In human social affairs, discrimination is treatment or consideration of, or making a distinction in favor of or against, a person based on the group, class, or category to which the person is perceived to belong rather than on individual attributes" (wikipedia)

For legal perspective, see Canadian Human Rights Act



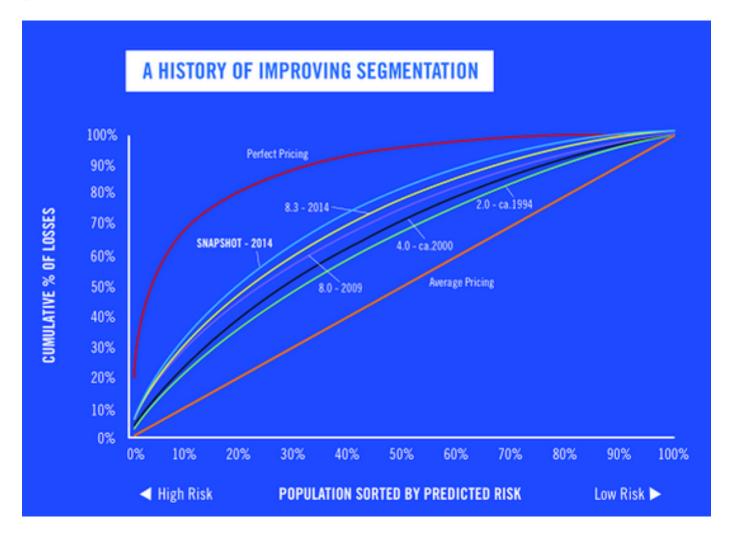








## **Model Comparison and Lorenz curves**



Source: Progressive Insurance



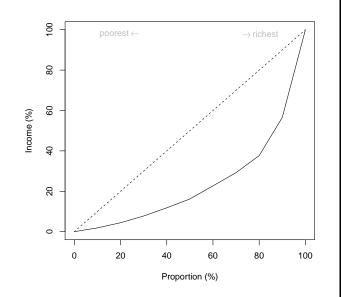
#### Model Comparison and Lorenz curves

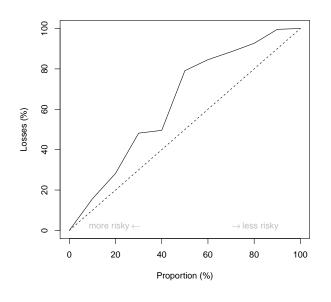
Consider an ordered sample  $\{y_1, \dots, y_n\}$  of incomes, with  $y_1 \leq y_2 \leq \dots \leq y_n$ , then Lorenz curve is

$$\{F_i, L_i\}$$
 with  $F_i = \frac{i}{n}$  and  $L_i = \frac{\sum_{j=1}^i y_j}{\sum_{j=1}^n y_j}$ 

We have observed losses  $y_i$  and premiums  $\widehat{\pi}(\boldsymbol{x}_i)$ . Consider an ordered sample by the model, see Frees, Meyers & Cummins (2014),  $\widehat{\pi}(\boldsymbol{x}_1) \geq \widehat{\pi}(\boldsymbol{x}_2) \geq \cdots \geq \widehat{\pi}(\boldsymbol{x}_n)$ , then plot

$$\{F_i, L_i\}$$
 with  $F_i = \frac{i}{n}$  and  $L_i = \frac{\sum_{j=1}^i y_j}{\sum_{j=1}^n y_j}$ 





#### Model Comparison for Life Insurance Models

Consider the case of a death insurance contract, that pays 1 if the insured deceased within the year.

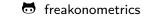
$$\pi(x) = \mathbb{E}\left[T_x \le t + 1|T_x > t\right]$$

- No price discrimination  $\pi = \mathbb{E}[\pi(X)]$
- Perfect discrimination  $\pi(x)$
- Imperfect discrimination

$$\pi_- = \mathbb{E}[\pi(X)|X < s] \text{ and } \pi_+ = \mathbb{E}[\pi(X)|X > s]$$

click to visualize the construction







#### From Econometric to 'Machine Learning' Techniques

In a competitive market, insurers can use different sets of variables and different models, e.g. GLMs,  $N_t | \mathbf{X} \sim \mathcal{P}(\lambda_{\mathbf{X}} \cdot t)$  and  $Y | \mathbf{X} \sim \mathcal{G}(\mu_{\mathbf{X}}, \varphi)$ 

$$\widehat{\pi}_{j}(\boldsymbol{x}) = \widehat{\mathbb{E}}\left[N_{1} \middle| \boldsymbol{X} = \boldsymbol{x}\right] \cdot \widehat{\mathbb{E}}\left[Y \middle| \boldsymbol{X} = \boldsymbol{x}\right] = \underbrace{\exp(\widehat{\boldsymbol{\alpha}}^{\mathsf{T}} \boldsymbol{x})}_{\text{Poisson } \mathcal{P}(\lambda_{\boldsymbol{x}})} \cdot \underbrace{\exp(\widehat{\boldsymbol{\beta}}^{\mathsf{T}} \boldsymbol{x})}_{\text{Gamma } \mathcal{G}(\mu_{\boldsymbol{X}}, \varphi)}$$

that can be extended to GAMs,

$$\widehat{\pi}_{j}(\boldsymbol{x}) = \exp\left(\sum_{k=1}^{d} \widehat{s}_{k}(x_{k})\right) \cdot \exp\left(\sum_{k=1}^{d} \widehat{t}_{k}(x_{k})\right)$$
Poisson  $\mathcal{P}(\lambda_{\boldsymbol{x}})$  Gamma  $\mathcal{G}(\mu_{\boldsymbol{X}}, \varphi)$ 

or some Tweedie model on  $S_t$  (compound Poisson, see Tweedie (1984)) conditional on X (see C. & Denuit (2005) or Kaas et al. (2008)) or any other statistical model

$$\widehat{\pi}_{j}(\boldsymbol{x}) \text{ where } \widehat{\pi}_{j} \in \underset{m \in \mathcal{F}_{j}: \mathcal{X}_{j} \to \mathbb{R}}{\operatorname{argmin}} \left\{ \sum_{i=1}^{n} \ell(s_{i}, m(\boldsymbol{x}_{i})) \right\}$$



#### From Econometric to 'Machine Learning' Techniques

For some loss function  $\ell : \mathbb{R}^2 \to \mathbb{R}_+$  (usually an  $L_2$  based loss,  $\ell(s, y) = (s - y)^2$  since argmin $\{\mathbb{E}[\ell(S, m)], m \in \mathbb{R}\}$  is  $\mathbb{E}(S)$ , interpreted as the pure premium).

For instance, consider regression trees, forests, neural networks, or boosting based techniques to approximate  $\pi(x)$ , and various techniques for variable selection, such as LASSO (see Hastie *et al.* (2009) or C., Flachaire & Ly (2017) for a description and a discussion).

With d competitors, each insured i has to choose among d premiums,  $\boldsymbol{\pi}_i = (\widehat{\pi}_1(\boldsymbol{x}_i), \cdots, \widehat{\pi}_d(\boldsymbol{x}_i)) \in \mathbb{R}^d_+$ .

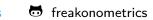




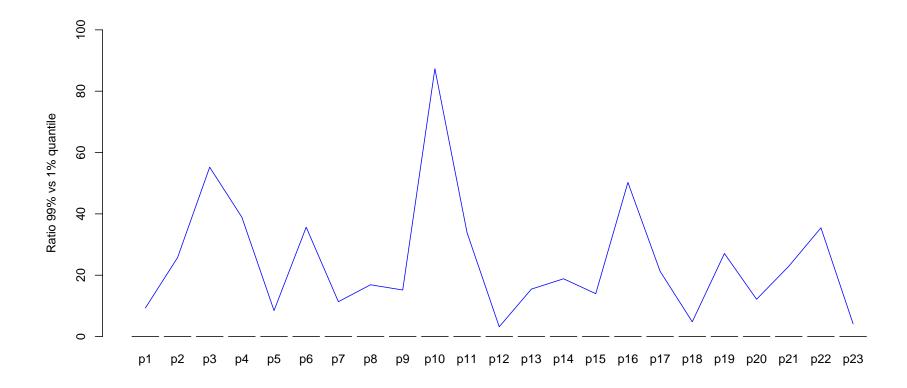


Insurance and Risk Segmentation: Pricing Game





## Insurance and Risk Segmentation: Pricing Game







**Insurance Ratemaking Before Competition** 

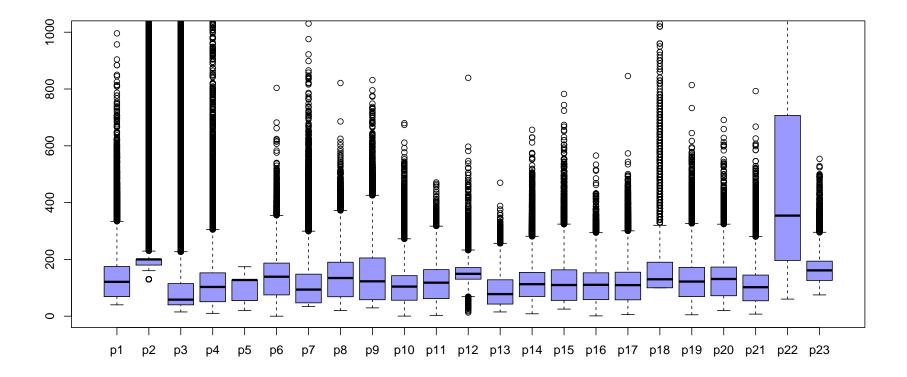






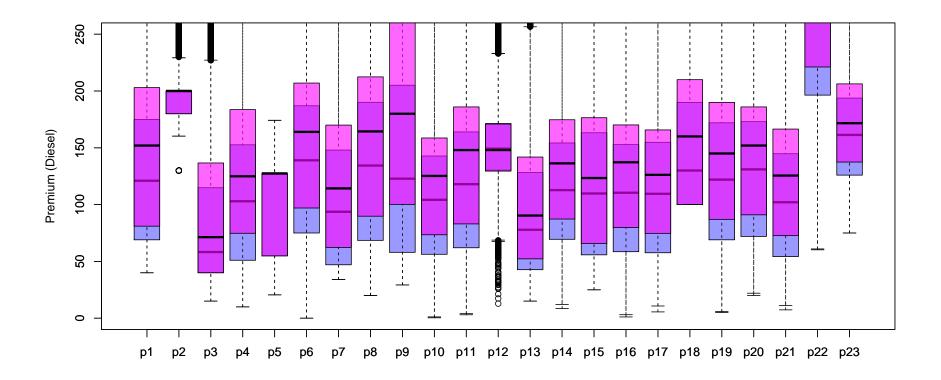


## **Insurance Ratemaking Before Competition**



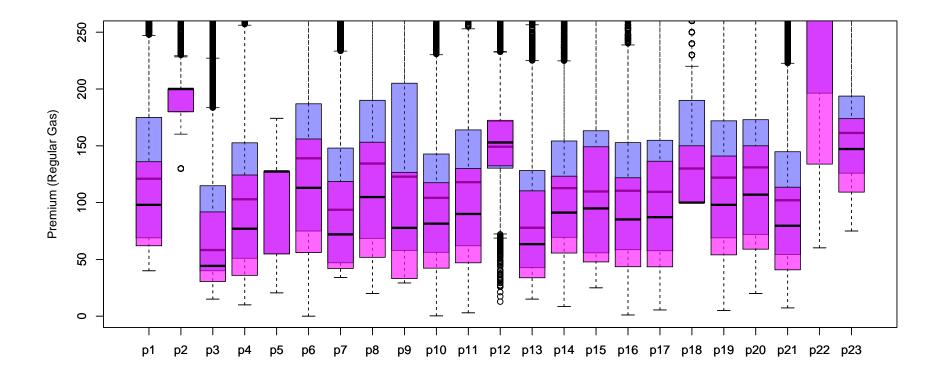


## **Insurance Ratemaking Before Competition Gas Type Diesel**



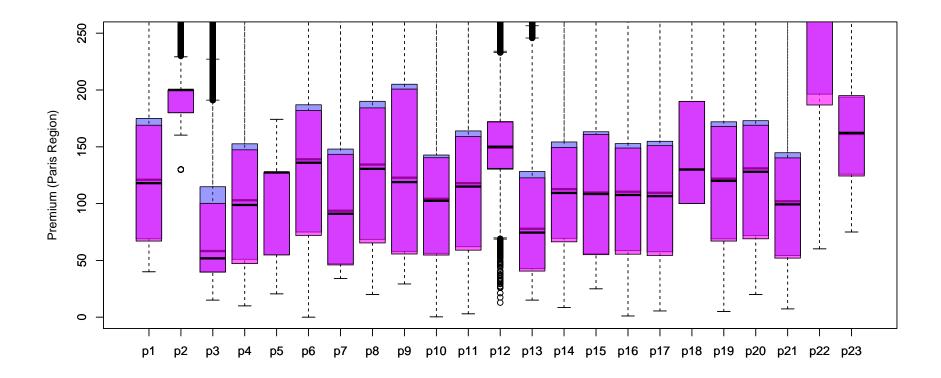


## Insurance Ratemaking Before Competition Gas Type Regular





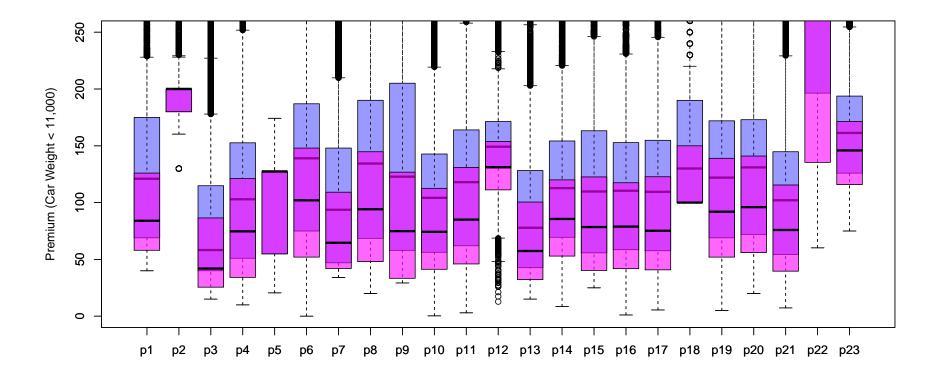
## **Insurance Ratemaking Before Competition Paris Region**





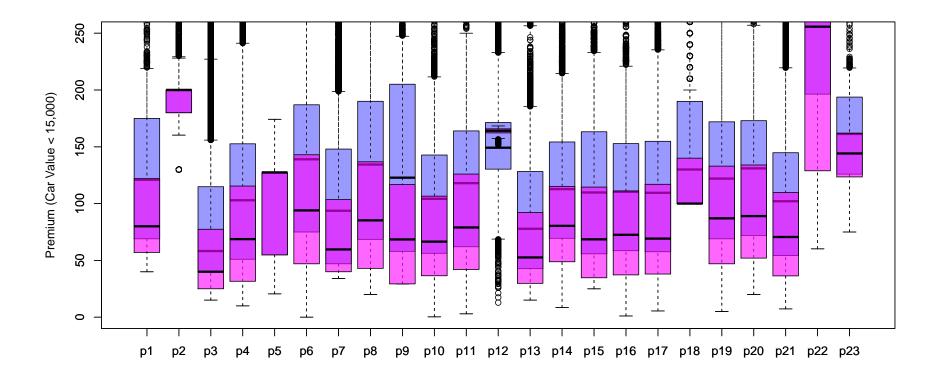


## Insurance Ratemaking Before Competition Car Weight





## Insurance Ratemaking Before Competition Car Value









## **Insurance Ratemaking Competition: Comonotonicity?** 800 Insurer 17 1000 1000 200 200 800 200 Insurer 13 Insurer 17 Insurer 10 Insurer 21 1.0 Insurer 13 Insurer 17 Insurer 10



# **Insurance Ratemaking Competition: Comonotonicity?** 800 Insurer 4 400 1000 1000 200 200 Insurer 3 Insurer 10 1.0 Insurer 3 Insurer 10



## **Insurance Ratemaking Competition**

We need a **Decision Rule** to select premium chosen by insured i

Ins1	Ins2	Ins3	Ins4	Ins5	Ins6
787.93	706.97	1032.62	907.64	822.58	603.83
170.04	197.81	285.99	212.71	177.87	265.13
473.15	447.58	343.64	410.76	414.23	425.23
337.98	336.20	468.45	339.33	383.55	672.91



## **Insurance Ratemaking Competition**

Basic 'rational rule'  $\pi_i = \min\{\widehat{\pi}_1(\boldsymbol{x}_i), \cdots, \widehat{\pi}_d(\boldsymbol{x}_i)\} = \widehat{\pi}_{1:d}(\boldsymbol{x}_i)$ 

	Ins1	Ins2	Ins3	Ins4	Ins5	Ins6
100	787.93	706.97	1032.62	907.64	822.58	603.83
	170.04	197.81	285.99	212.71	177.87	265.13
	473.15	447.58	343.64	410.76	414.23	425.23
	337.98	336.20	468.45	339.33	383.55	672.91



## **Insurance Ratemaking Competition**

A more realistic rule  $\pi_i \in \{\widehat{\pi}_{1:d}(\boldsymbol{x}_i), \widehat{\pi}_{2:d}(\boldsymbol{x}_i), \widehat{\pi}_{3:d}(\boldsymbol{x}_i)\}$ 

Ins1	Ins2	Ins3	Ins4	Ins5	Ins6
787.93	706.97	1032.62	907.64	822.58	603.83
170.04	197.81	285.99	212.71	177.87	265.13
473.15	447.58	343.64	410.76	414.23	425.23
337.98	336.20	468.45	339.33	383.55	672.91



#### A Game with Rules... but no Goal

```
Two datasets: a training one, and a pricing one (without the losses in the later)
```

**Step 1**: provide premiums to all contracts in the pricing dataset

Step 2: allocate insured among players

Season 1 13 players

Season 2 14 players

**Step 3** [season 2]: provide additional information (premiums of competitors)

**Season 3** 23 players (3 markets, 8+8+7)

Step 3-6 [season 3] : dynamics, 4 years

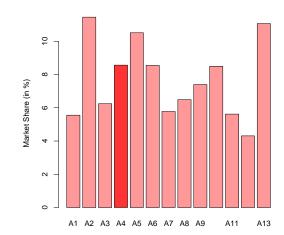
actinfo.

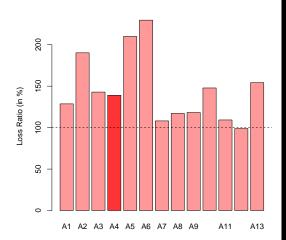


#### Insurer 4

GLM for frequency and standard cost (large claimes were removed, above 15k), Interaction Age and Gender

Actuary working for a mutuelle company

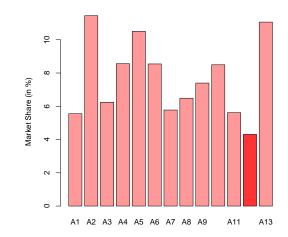


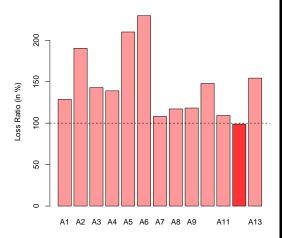


#### Insurer 11

Use of two XGBoost models (bodily injury and material), with correction for negative premiums

Actuary working for a private insurance company



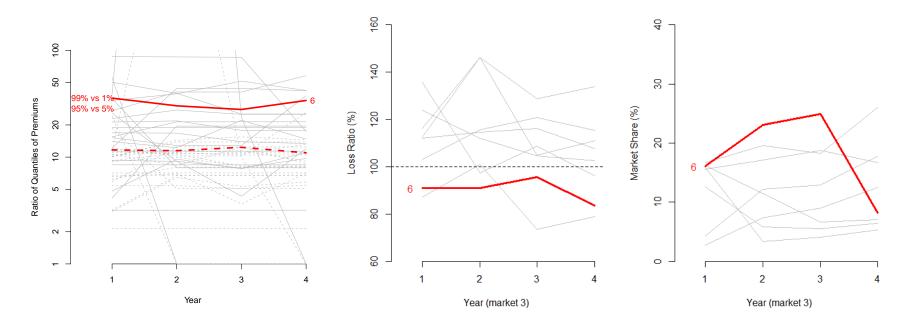




Insurer 6 (market 3)

Team of two actuaries (degrees in Engineering and Physics), in Vancouver, Canada. Used GLMs (Tweedie), no territorial classification, no use of information about other competitors

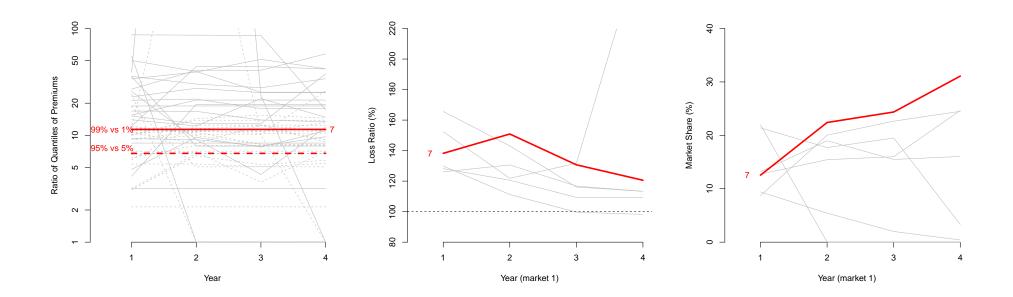
"Segments with high market share and low loss ratios were also given some premium increase"



actinfo.

Insurer 7 (market 1)

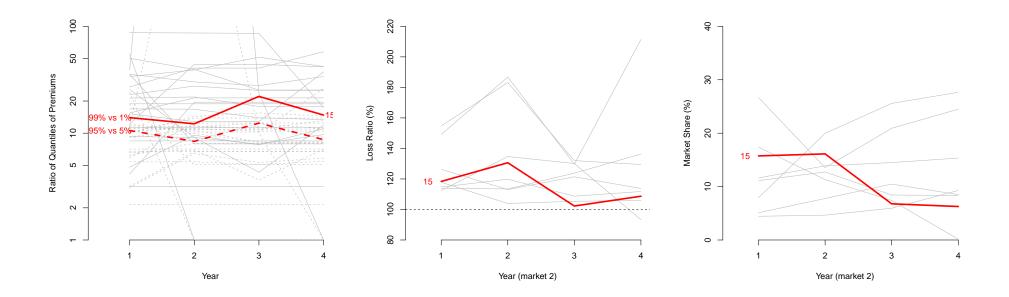
Actuary in France, used random forest for variable selection, and GLMs





Insurer 15 (market 2)

Actuary, working as a consultant, Margin Method with iterations, MS Access & MS Excel





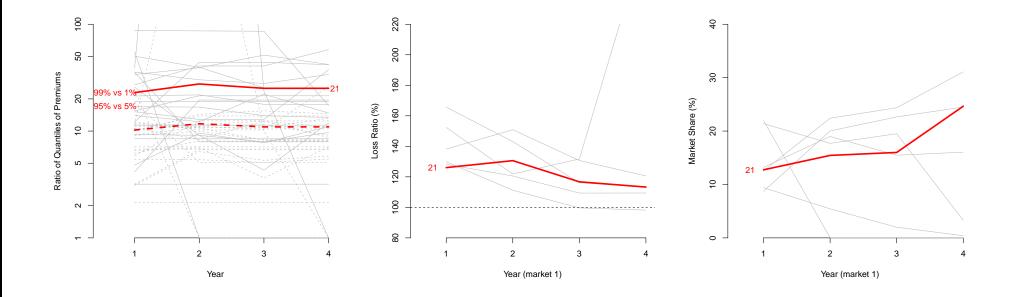




Insurer 21 (market 1)

Actuary, working as a consultant, used GLMs, with variable selection using LARS and LASSO

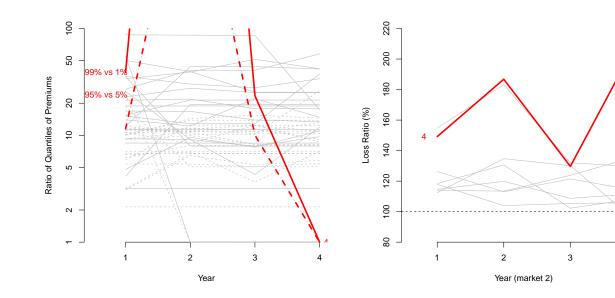
Iterative learning algorithm (codes available on github)

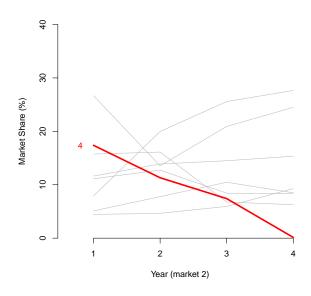




Insurer 4 (market 2)

Actuary, working as a consultat, used XGBOOST, used GLMs for year 3.



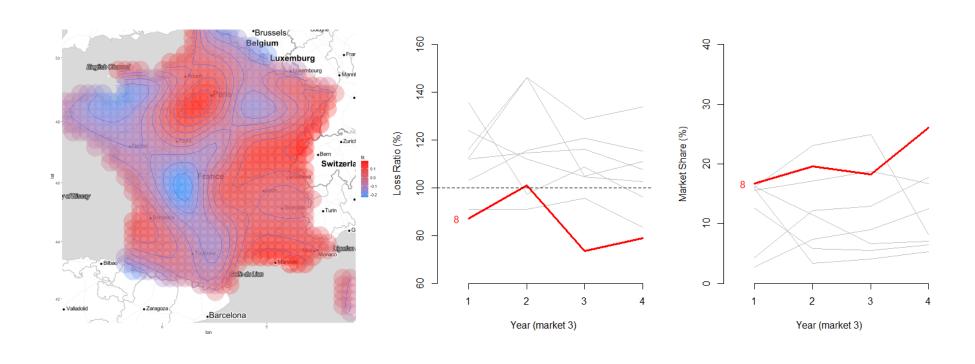




Insurer 8 (market 3)

Mathematician, working on Solvency II sofware in Austria

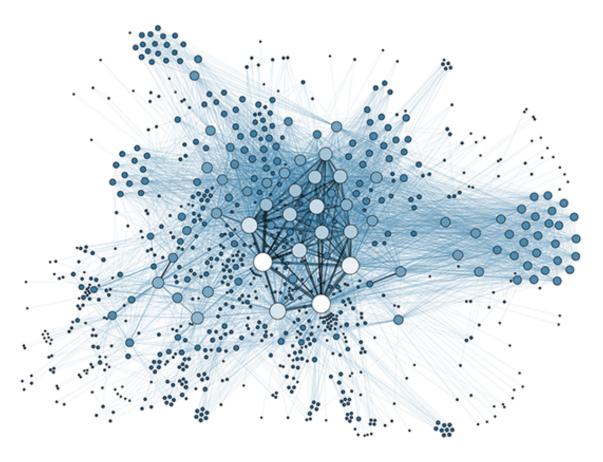
Generalized Additive Models with spatial variable





# Cluster, Segmentation and (Social) Networks

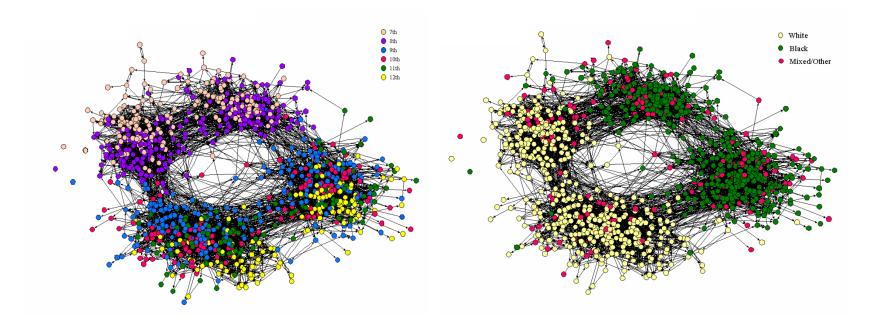
Social networks could be used to get additional information about insured people...



Why not using social networks to create (more) solidarity?

## Cluster, Segmentation and (Social) Networks

Homophily is the tendency of individuals to associate and bond with similar others, "birds of a feather flock together"



from Moody (2001) Race, School Integration and Friendship Segregation in America

actinfo

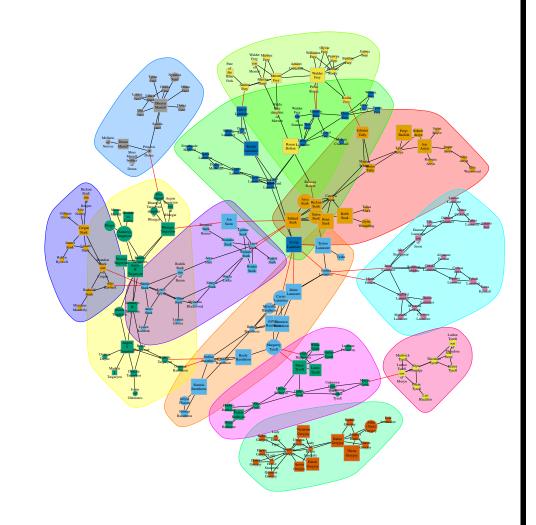
# Cluster, Segmentation and (Social) Networks

So far, risk classes are based on covariates X, correlated (causal effect?) with claims occurrence (or severity).

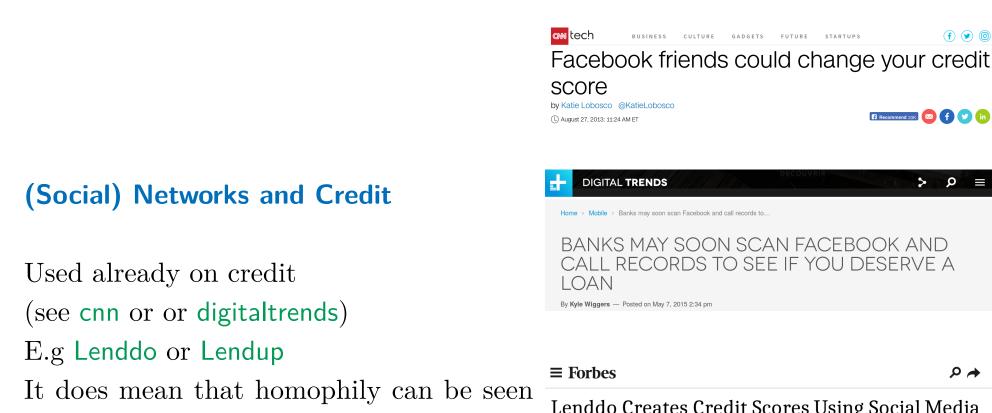
Why not consider clusters in (social) networks, too?

A lot of cofounding variables (age, profession, location, etc.)

See InsPeer experience.



via shiring.github.io



Lenddo Creates Credit Scores Using Social Media



INVESTOPEDIA **≡** Q 1

LendUp: A Responsible Alternative To Payday Loans?

By Amy Fontinelle | April 7, 2015 — 2:40 PM EDT



tory' variales...

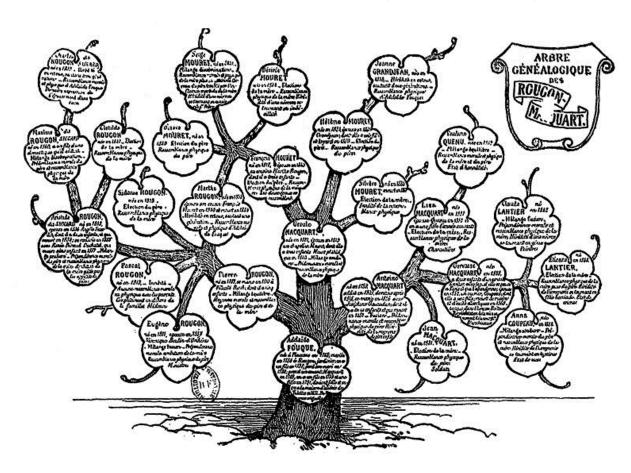
as a substitute to standard credit 'explana-

2

Recommend 33K 🖂 f 🕥 in

#### **Information and Networks**

But other kinds of networks can be used, e.g. (genealogical) trees



See Ewen Gallic's ongoing work (actinfo chair).



#### **Privacy Issues**

See General Data Protection Regulation (EU 2016/679): what about aggregation?

Consider a population  $\{1, \dots, n\}$  and a partition  $\{\mathcal{I}_1, \dots, \mathcal{I}_k\}$  (e.g. geographical areas Z), with respective sizes  $\{n_1, \dots, n_k\}$ . Set  $\overline{Y}_j = \frac{1}{n_j} \sum_{i \in I_j} Y_i$ .

For continous covariates, set 
$$\overline{X}_{k,j} = \frac{1}{n_k} \sum_{i \in I_j} X_{k,i}$$
,

For categorical variables, consider the associate composition variable

$$\overline{\boldsymbol{X}}_{k,j} = (\overline{X}_{k,1,j}, \cdots, \overline{X}_{k,d_k,j}) \text{ where } \overline{X}_{k,\ell,j} = \frac{1}{n_k} \sum_{i \in I_j} \mathbf{1}(X_{k,i} = \ell).$$

See e.g. C. & Pigeon (2016) on micro-macro models and Enora Belz's ongoing work.

# **Privacy Issues**

See Verbelen, Antonio & Claeskens (2016) and Antonio & C. (2017) on GPS data

	Predictor		Classic		Time-hybrid		Meter-hybrid		Telematics	
	Time	×	offset	×	offset					
Policy	Age									
	Experience	X	×	×	×	X	×			
	Sex	×	×							
	Material	×	×	×	×	×	×			
	Postal code	×	×	X	×	×	×			
	Bonus-malus	×	×	X	×	×	×			
	Age vehicle	×	×	X	×	×	×			
	Kwatt			X	×	×	×			
	Fuel	X	×	×		×				
Telematics	Distance					×	offset	X	offset	
	Yearly distance			X	×					
	Average distance			X	×	×	×			
	Road type 1111			X	×	×	×	×	×	
	Road type 1110			×	×	×	×	×	×	
	Time slot			X	×	×	×	×	×	
	Week/weekend			×	×	×	×	×	×	

